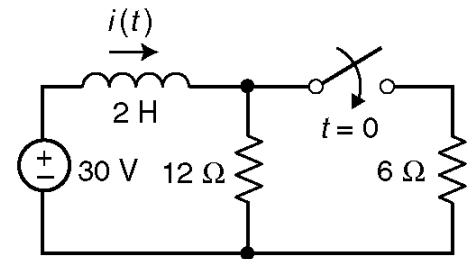


## ES 250 2nd Midterm Exam - Fall 2013

Name \_\_\_\_\_ k6 \_\_\_\_\_

Student # \_\_\_\_\_

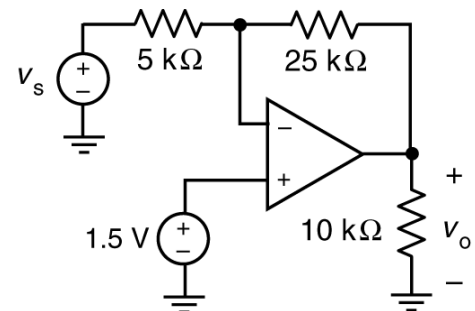
1. The switch in this circuit closes at time  $t = 0$ . Let  $i(0)$  denote the inductor current when the switch is open and the circuit is at steady state. Similarly, let  $i(\infty)$  denote the steady state inductor current when the switch is closed.



Determine the values of  $i(0)$  and  $i(\infty)$ :

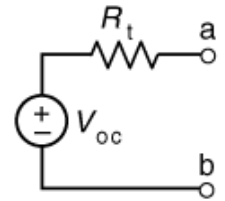
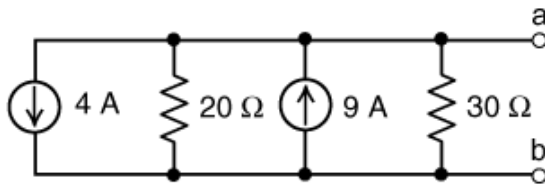
$$i(0) = \underline{\underline{2.5}} \text{ A and } i(\infty) = \underline{\underline{7.5}} \text{ A.}$$

2. The input to this circuit is the voltage  $v_s$ . The output is the voltage  $v_o$ . The output is related to the input by the equation  $v_o = m v_s + b$  where  $m$  and  $b$  are constants. The values of  $m$  and  $b$  are:



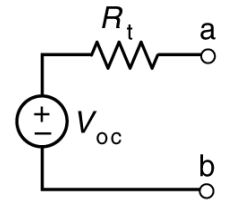
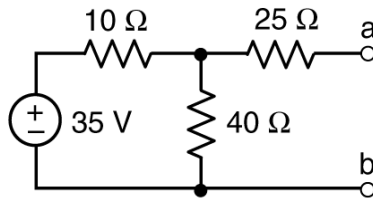
$$m = \underline{\underline{-5}} \text{ V/V and } b = \underline{\underline{9}} \text{ V.}$$

3. Here's a circuit and its Thevenin equivalent circuit. Determine the values of the Thevenin resistance,  $R_t$ , and of the open-circuit voltage,  $V_{oc}$ .



$$R_t = \underline{\quad 12 \quad} \Omega \text{ and } V_{oc} = \underline{\quad 60 \quad} \text{V}$$

4. Here's a circuit and its Thevenin equivalent circuit. Determine the values of the Thevenin resistance,  $R_t$ , and of the open-circuit voltage,  $V_{oc}$ .



$$R_t = \underline{\quad 33 \quad} \Omega \text{ and } V_{oc} = \underline{\quad 28 \quad} \text{V}$$

5. Given that  $0 \leq R \leq \infty$  in this circuit, and given these two observations:

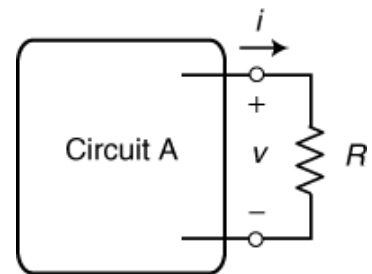
When  $R = 0$  then  $i = 1.5 \text{ A}$ .

When  $R = \infty$  then  $v = 24 \text{ V}$ .

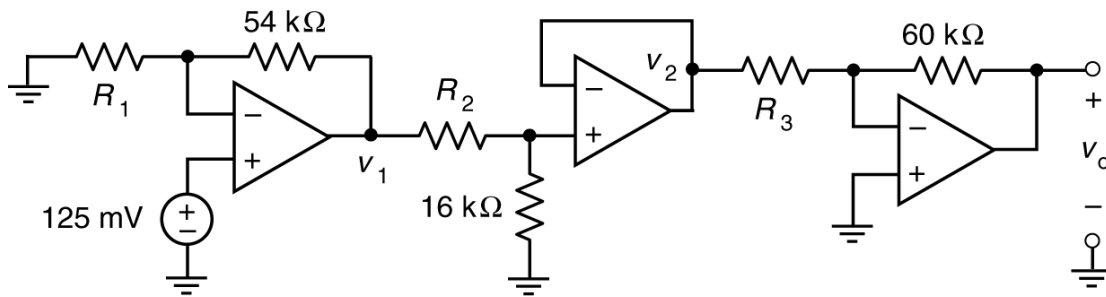
Fill in the blanks in the following statements:

a) When  $R = \underline{\quad 1.4545 \quad} \Omega$  then  $v = 2 \text{ V}$ .

a) When  $R = \underline{\quad 104 \quad} \Omega$  then  $i = 0.20 \text{ A}$ .



6.



The values of the node voltages  $v_1$ ,  $v_2$  and  $v_0$ , are  $v_1 = 875$  mV,  $v_2 = 350$  mV and  $v_0 = -600$  mV. Determine the value of the resistances  $R_1$ ,  $R_2$  and  $R_3$ :

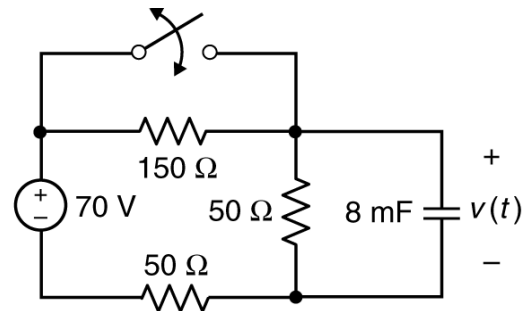
$$R_1 = \underline{\quad 9 \quad} \text{ k}\Omega, \quad R_2 = \underline{\quad 24 \quad} \text{ k}\Omega \text{ and } R_3 = \underline{\quad 35 \quad} \text{ k}\Omega.$$

7. a) Determine the time constant,  $\tau$ , and the steady state capacitor voltage,  $v(\infty)$ , when the switch is **open**:

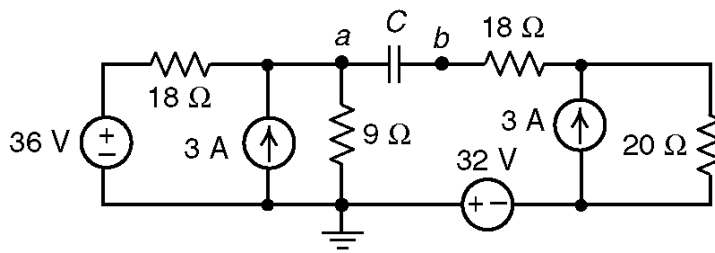
$$\tau = \underline{\quad 320 \quad} \text{ ms} \text{ and } v(\infty) = \underline{\quad 14 \quad} \text{ V}$$

b) Determine the time constant,  $\tau$ , and the steady state capacitor voltage,  $v(\infty)$ , when the switch is **closed**:

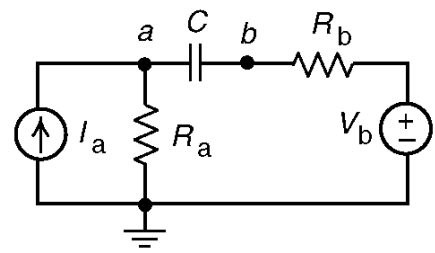
$$\tau = \underline{\quad 200 \quad} \text{ ms} \text{ and } v(\infty) = \underline{\quad 35 \quad} \text{ V}$$



8.



original circuit



equivalent circuit

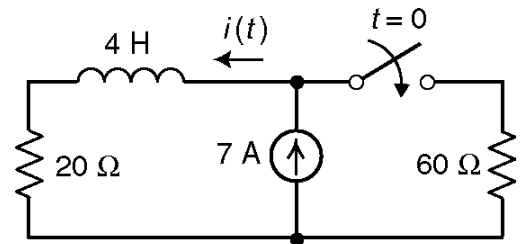
The equivalent circuit on the right is obtained from the original circuit on the left using source transformations and equivalent resistances. (The lower case letters  $a$  and  $b$  identify the nodes of the capacitor in both the original and equivalent circuits.) Determine the values of  $R_a$ ,  $I_a$ ,  $R_b$  and  $V_b$  in the equivalent circuit:

$$R_a = \underline{6} \Omega, \quad I_a = \underline{5} \text{ A}, \quad R_b = \underline{38} \Omega \quad \text{and} \quad V_b = \underline{28} \text{ V}.$$

9. This circuit is at steady state before the switch closes. The inductor current can be represented as

$$i(t) = A + B e^{-at} \text{ Amps for } t > 0$$

Determine the values of the real constants  $A$ ,  $B$  and  $a$ :



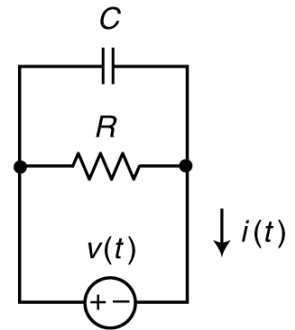
$$A = \underline{5.25} \text{ Amps}, \quad B = \underline{1.75} \text{ Amps} \quad \text{and} \quad a = \underline{20} \text{ 1/s}.$$

10. The input to this circuit is the voltage:  $v(t) = 20 + 4e^{-7t}$  V for  $t > 0$

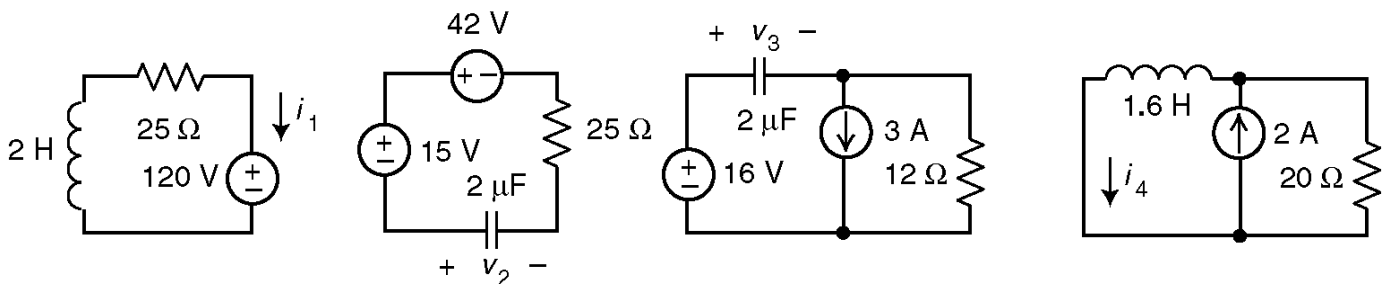
The output is the current:  $i(t) = 4 - 2.7e^{-7t}$  A for  $t > 0$

Determine the values of the resistance and capacitance:

$$R = \underline{\quad 5 \quad} \Omega \quad \text{and} \quad C = \underline{\quad 125 \quad} \text{mF}.$$

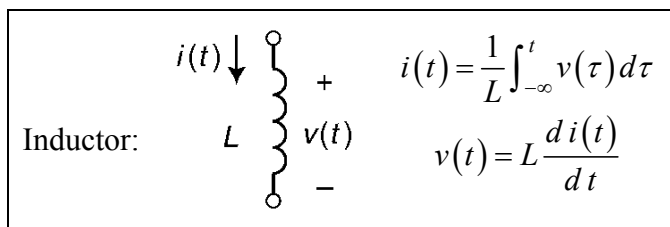
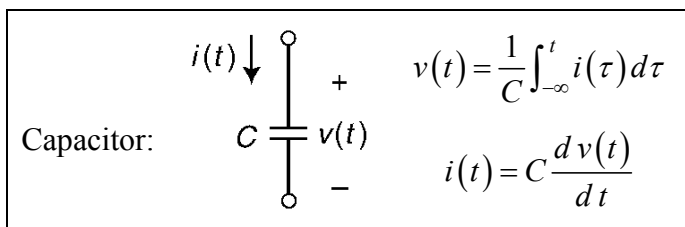


11. Here are 4 separate dc circuits. Because they are dc circuits, the capacitors in these circuits act like open circuits and the inductors act like short circuits. Determine the values of  $i_1$ ,  $v_2$ ,  $v_3$  and  $i_4$ .



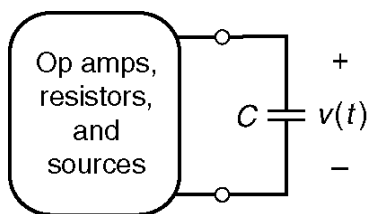
$$i_1 = \underline{\quad -4.8 \quad} \text{A}, \quad v_2 = \underline{\quad 27 \quad} \text{V}, \quad v_3 = \underline{\quad 52 \quad} \text{V} \quad \text{and} \quad i_4 = \underline{\quad 2 \quad} \text{A}.$$

## Element Equations

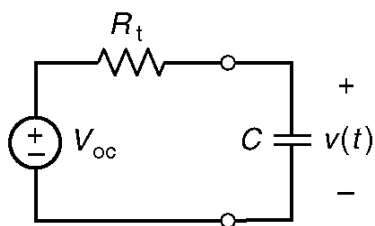


## First-Order Circuits

### FIRST-ORDER CIRCUIT CONTAINING A CAPACITOR



Replace the circuit consisting of op amps, resistors, and sources by its Thévenin equivalent circuit:



The capacitor voltage is:

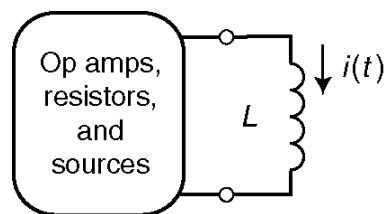
$$v(t) = V_{oc} + (v(0) - V_{oc}) e^{-\frac{t}{\tau}}$$

where the time constant,  $\tau$ , is

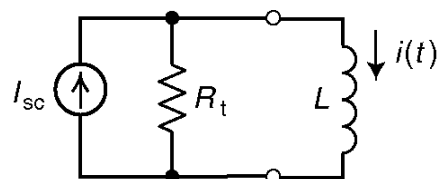
$$\tau = R_t C$$

and the initial condition,  $v(0)$ , is the capacitor voltage at time  $t = 0$ .

### FIRST-ORDER CIRCUIT CONTAINING AN INDUCTOR



Replace the circuit consisting of op amps, resistors, and sources by its Norton equivalent circuit:



The inductor current is

$$i(t) = I_{sc} + (i(0) - I_{sc}) e^{-\frac{t}{\tau}}$$

where the time constant,  $\tau$ , is

$$\tau = \frac{L}{R_t}$$

and the initial condition,  $i(0)$ , is the inductor current at time  $t = 0$ .