

## ES 250 2nd Midterm Exam - Fall 2013

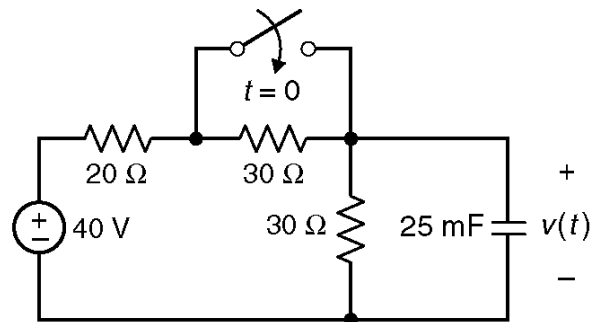
Name \_\_\_\_\_ k3 \_\_\_\_\_

Student # \_\_\_\_\_

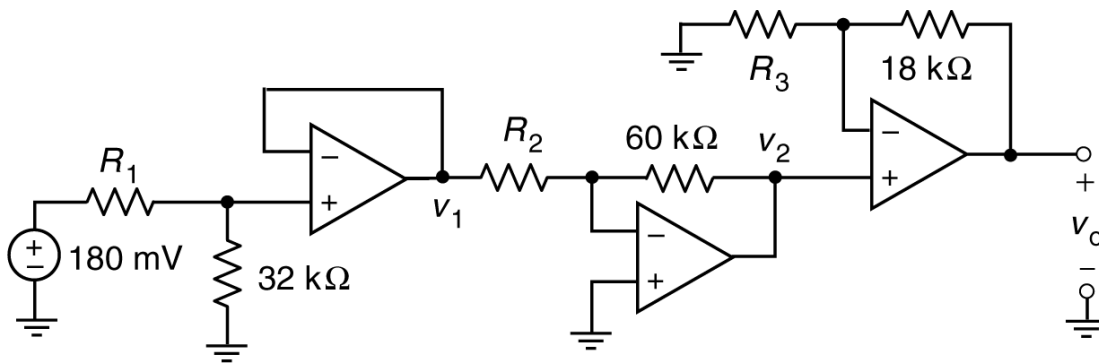
1. The switch in this circuit closes at time  $t = 0$ . Let  $v(0)$  denote the capacitor voltage when the switch is open and the circuit is at steady state. Similarly, let  $v(\infty)$  denote the steady state capacitor voltage when the switch is closed.

Determine the values of  $v(0)$  and  $v(\infty)$ :

$$v(0) = \underline{15} \text{ V and } v(\infty) = \underline{24} \text{ V.}$$



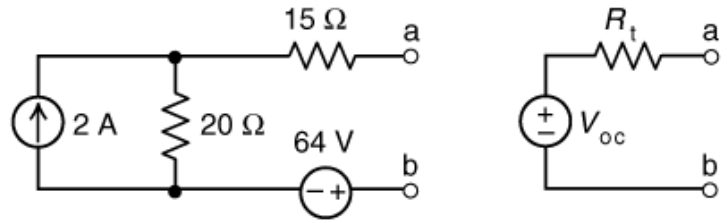
2.



The values of the node voltages  $v_1$ ,  $v_2$  and  $v_0$ , are  $v_1 = 80 \text{ mV}$ ,  $v_2 = -320 \text{ mV}$  and  $v_0 = -960 \text{ mV}$ . Determine the value of the resistances  $R_1$ ,  $R_2$  and  $R_3$ :

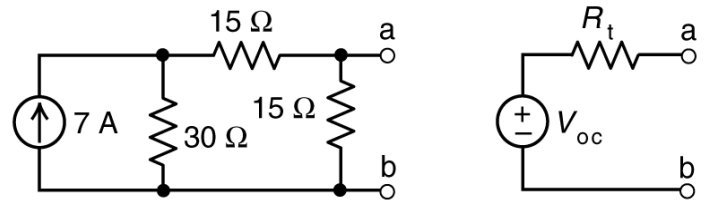
$$R_1 = \underline{40} \text{ k}\Omega, \quad R_2 = \underline{15} \text{ k}\Omega \text{ and } R_3 = \underline{9} \text{ k}\Omega.$$

3. Here's a circuit and its Thevenin equivalent circuit. Determine the values of the Thevenin resistance,  $R_t$ , and of the open-circuit voltage,  $V_{oc}$ .



$$R_t = \underline{35} \ \Omega \text{ and } V_{oc} = \underline{-24} \ \text{V}$$

4. Here's a circuit and its Thevenin equivalent circuit. Determine the values of the Thevenin resistance,  $R_t$ , and of the open-circuit voltage,  $V_{oc}$ .



$$R_t = \underline{11.25} \ \Omega \text{ and } V_{oc} = \underline{52.5} \ \text{V}$$

5. Given that  $0 \leq R \leq \infty$  in this circuit, and given these two observations:

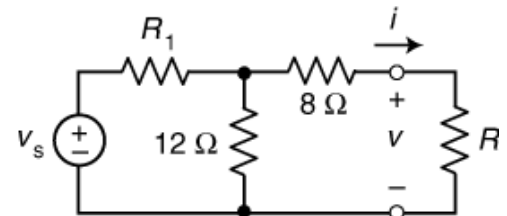
When  $R = 0$  then  $i = 1.5 \text{ A}$ .

When  $R = \infty$  then  $v = 24 \text{ V}$ .

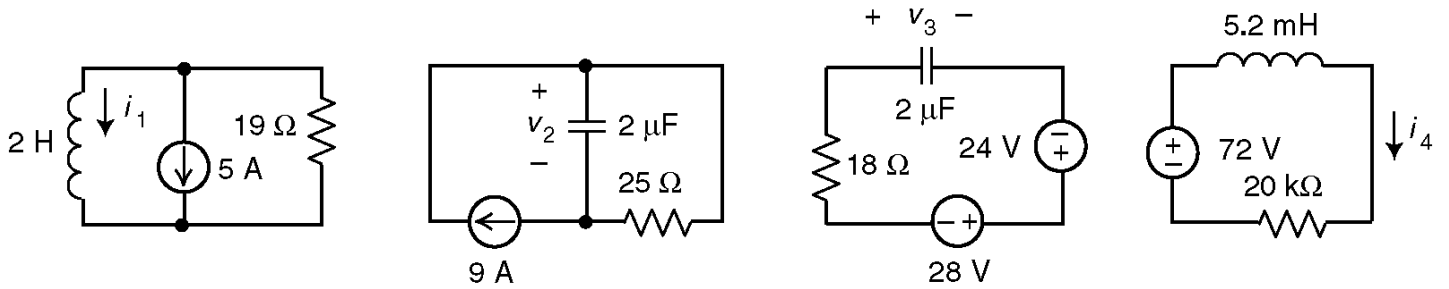
Fill in the blanks in the following statements:

a) When  $R = \underline{8} \ \Omega$  then  $v = 8 \text{ V}$ .

b) When  $R = \underline{24} \ \Omega$  then  $i = 0.6 \text{ A}$ .

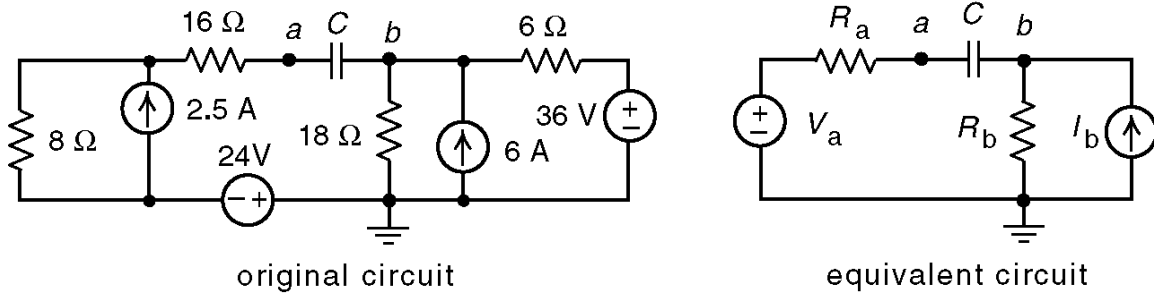


6. Here are 4 separate dc circuits. Because they are dc circuits, the capacitors in these circuits act like open circuits and the inductors act like short circuits. Determine the values of  $i_1$ ,  $v_2$ ,  $v_3$  and  $i_4$ .



$i_1 = \underline{-5} \text{ A}$ ,  $v_2 = \underline{225} \text{ V}$ ,  $v_3 = \underline{-4} \text{ V}$  and  $i_4 = \underline{3.6} \text{ mA}$ .

7.



The equivalent circuit on the right is obtained from the original circuit on the left using source transformations and equivalent resistances. (The lower case letters  $a$  and  $b$  identify the nodes of the capacitor in both the original and equivalent circuits.) Determine the values of  $R_a$ ,  $V_a$ ,  $R_b$  and  $I_b$  in the equivalent circuit:

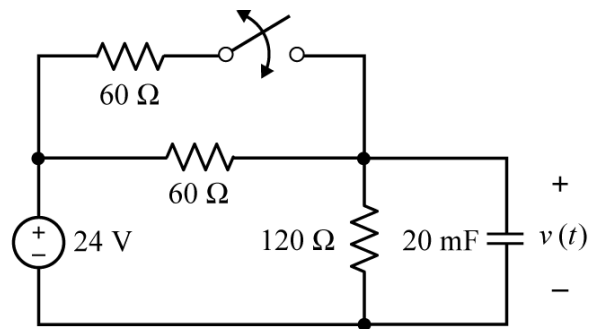
$R_a = \underline{24} \text{ } \Omega$ ,  $V_a = \underline{-4} \text{ V}$ ,  $R_b = \underline{4.5} \text{ } \Omega$  and  $I_b = \underline{12} \text{ A}$ .

8. a) Determine the time constant,  $\tau$ , and the steady state capacitor voltage,  $v(\infty)$ , when the switch is **open**:

$$\tau = \underline{\quad 0.8 \quad} \text{ s} \quad \text{and} \quad v(\infty) = \underline{\quad 16 \quad} \text{ V}$$

b) Determine the time constant,  $\tau$ , and the steady state capacitor voltage,  $v(\infty)$ , when the switch is **closed**:

$$\tau = \underline{\quad 0.48 \quad} \text{ s} \quad \text{and} \quad v(\infty) = \underline{\quad 19.2 \quad} \text{ V}$$

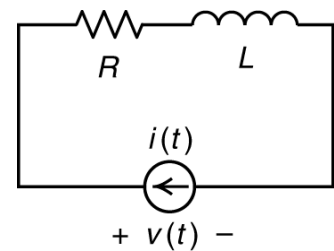


9. The input to this circuit is the current:  $i(t) = 5 + 2e^{-7t}$  A for  $t > 0$

The output is the voltage:  $v(t) = 75 - 82e^{-7t}$  V for  $t > 0$

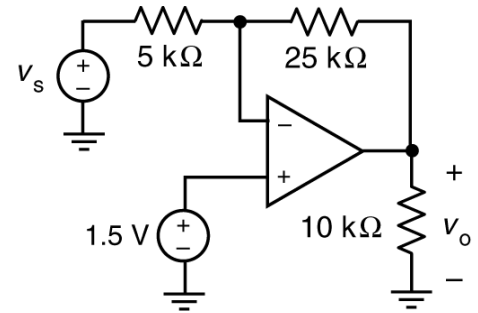
Determine the values of the resistance and inductance:

$$R = \underline{\quad 15 \quad} \Omega \quad \text{and} \quad L = \underline{\quad 8 \quad} \text{ H.}$$



**10.** The input to this circuit is the voltage  $v_s$ . The output is the voltage  $v_o$ . The output is related to the input by the equation  $v_o = m v_s + b$  where  $m$  and  $b$  are constants. The values of  $m$  and  $b$  are:

$$m = \underline{-5} \text{ V/V and } b = \underline{9} \text{ V.}$$

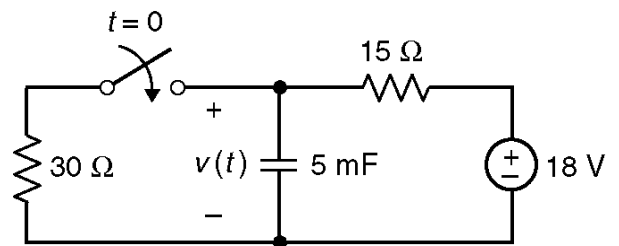


**11.** This circuit is at steady state before the switch closes. The capacitor voltage can be represented as

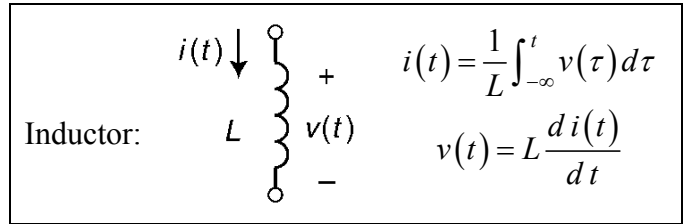
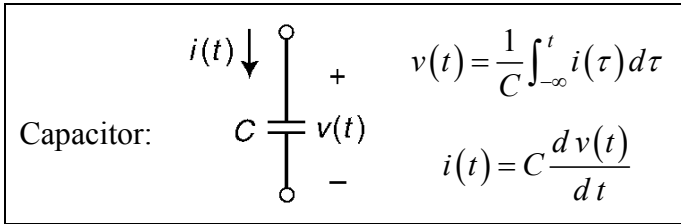
$$v(t) = A + B e^{-at} \text{ V for } t > 0$$

Determine the values of the real constants  $A$ ,  $B$  and  $a$ :

$$A = \underline{12} \text{ V, } B = \underline{6} \text{ V and } a = \underline{20} \text{ 1/s.}$$

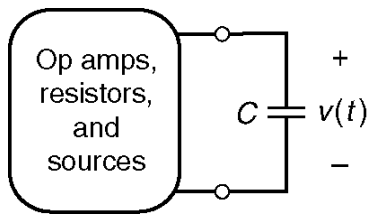


## Element Equations

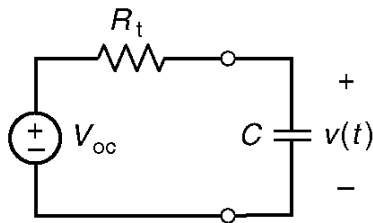


## First-Order Circuits

### FIRST-ORDER CIRCUIT CONTAINING A CAPACITOR



Replace the circuit consisting of op amps, resistors, and sources by its Thévenin equivalent circuit:



The capacitor voltage is:

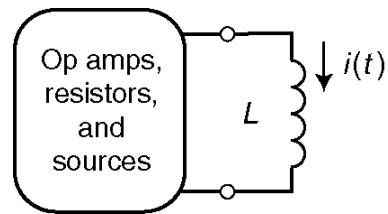
$$v(t) = V_{oc} + (v(0) - V_{oc}) e^{-\frac{t}{\tau}}$$

where the time constant,  $\tau$ , is

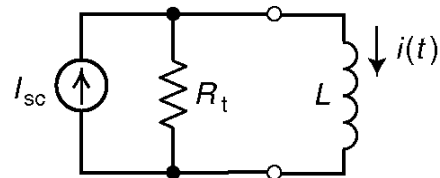
$$\tau = R_t C$$

and the initial condition,  $v(0)$ , is the capacitor voltage at time  $t = 0$ .

### FIRST-ORDER CIRCUIT CONTAINING AN INDUCTOR



Replace the circuit consisting of op amps, resistors, and sources by its Norton equivalent circuit:



The inductor current is

$$i(t) = I_{sc} + (i(0) - I_{sc}) e^{-\frac{t}{\tau}}$$

where the time constant,  $\tau$ , is

$$\tau = \frac{L}{R_t}$$

and the initial condition,  $i(0)$ , is the inductor current at time  $t = 0$ .